

Notation/background on trees \mathcal{T}

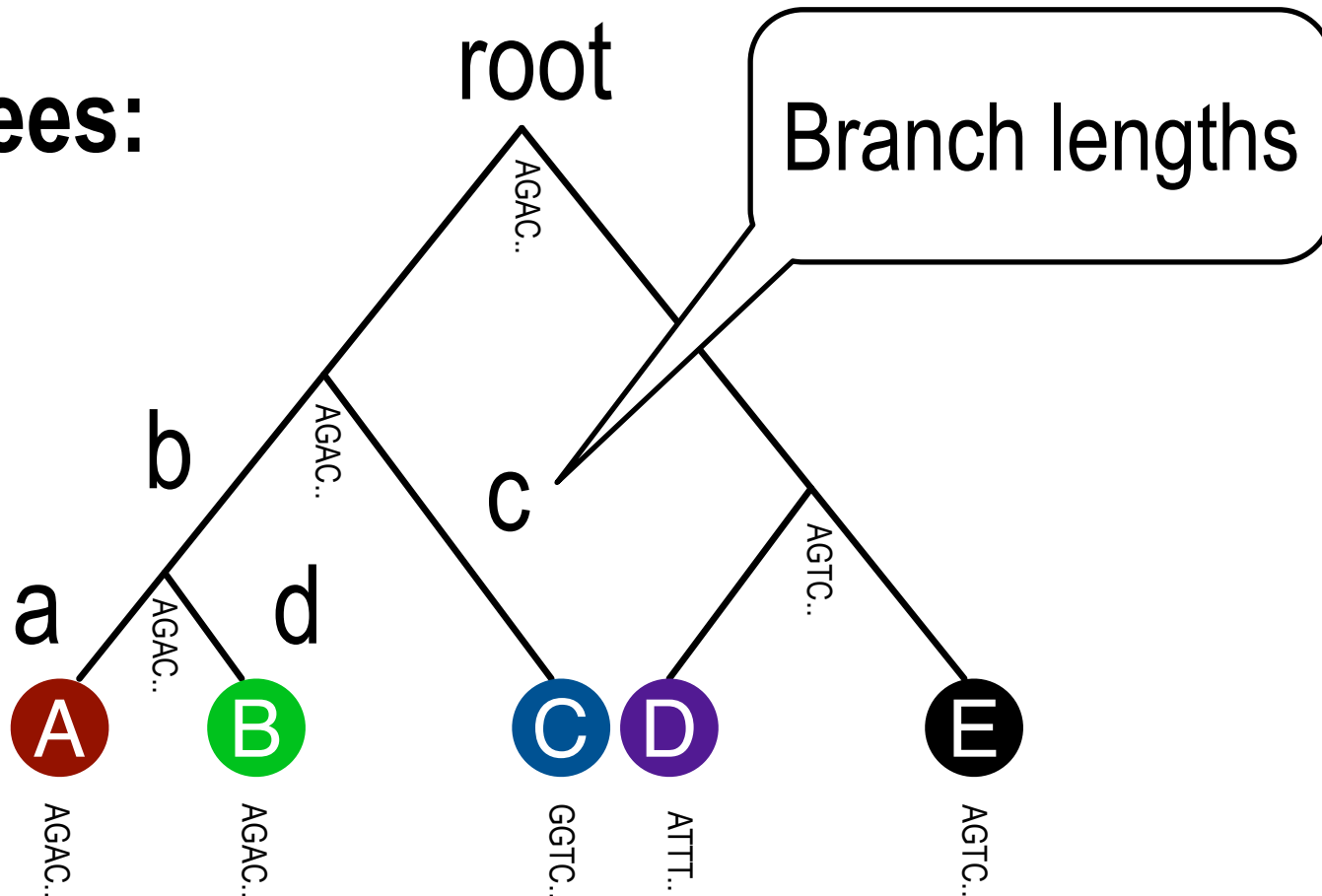
Clock trees:

$$a+b = c$$

$$d+b = c$$

$$a = d$$

...



Hidden sequences

Observations

Notation/background on trees \mathcal{T}

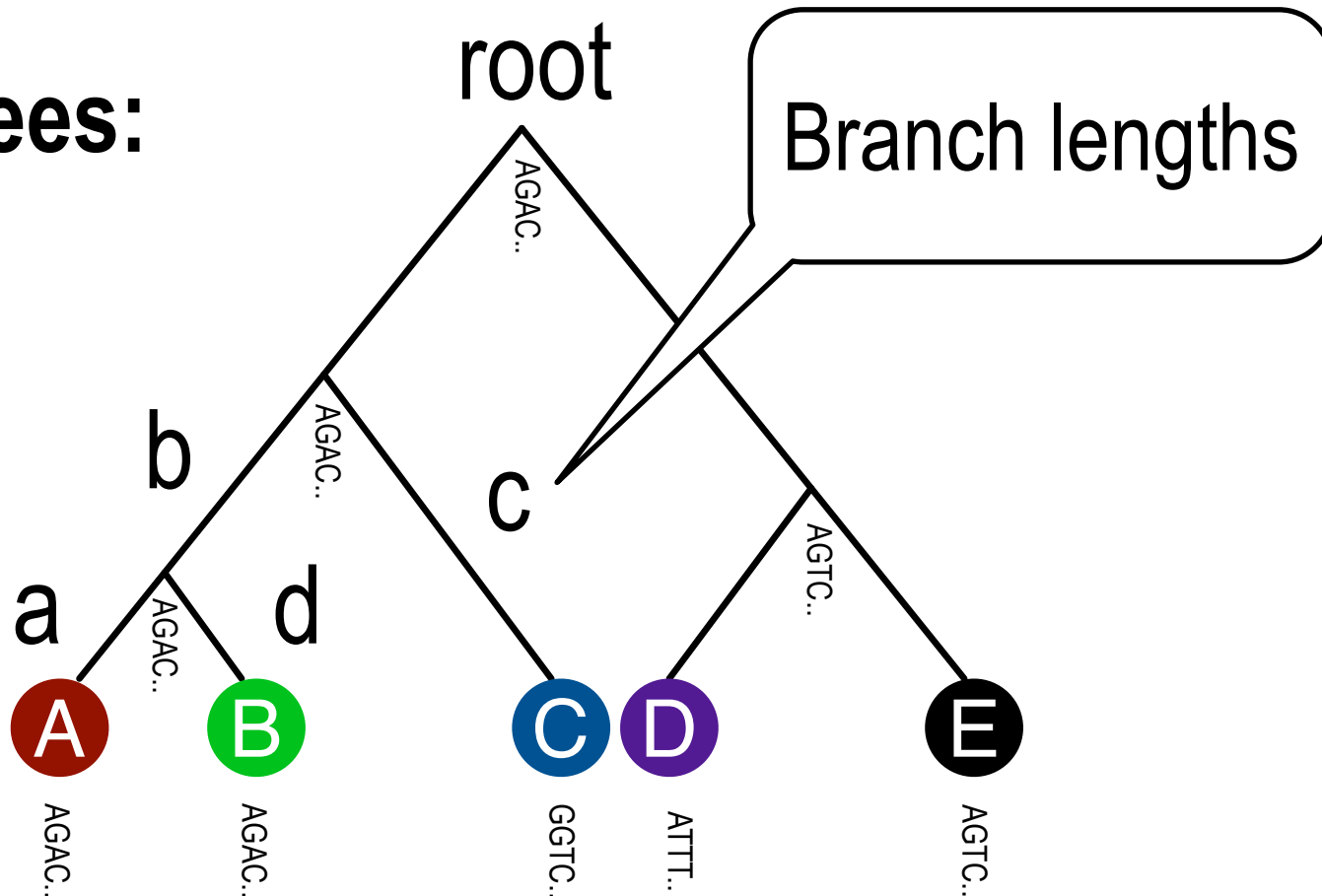
Clock trees:

$$a+b = c$$

$$d+b = c$$

$$a = d$$

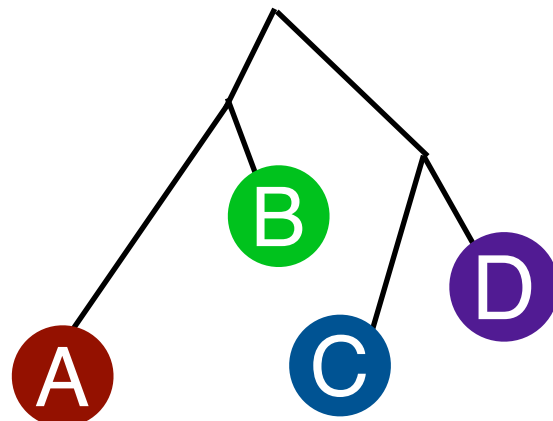
...



Hidden sequences

Observations

Non-clock tree:
remove additivity
restrictions on
branch lengths



Notation for our goals

Given a model (joint)...: $\gamma_t(\mathbf{x}_t) = p(\mathbf{x}_t, \mathbf{y}_t)$

Sample from a *target distribution*: $\pi_t(\mathbf{x}_t) = p(\mathbf{x}_t | \mathbf{y}_t)$

$$\pi_t(\mathbf{x}_t) = \frac{\gamma_t(\mathbf{x}_t)}{Z_t}$$

.. and/or evaluate the normalization: $Z = p(\mathbf{y}_t)$

Notation

\mathcal{X}

State space

$x_t \in \mathcal{X}$

Point in that space

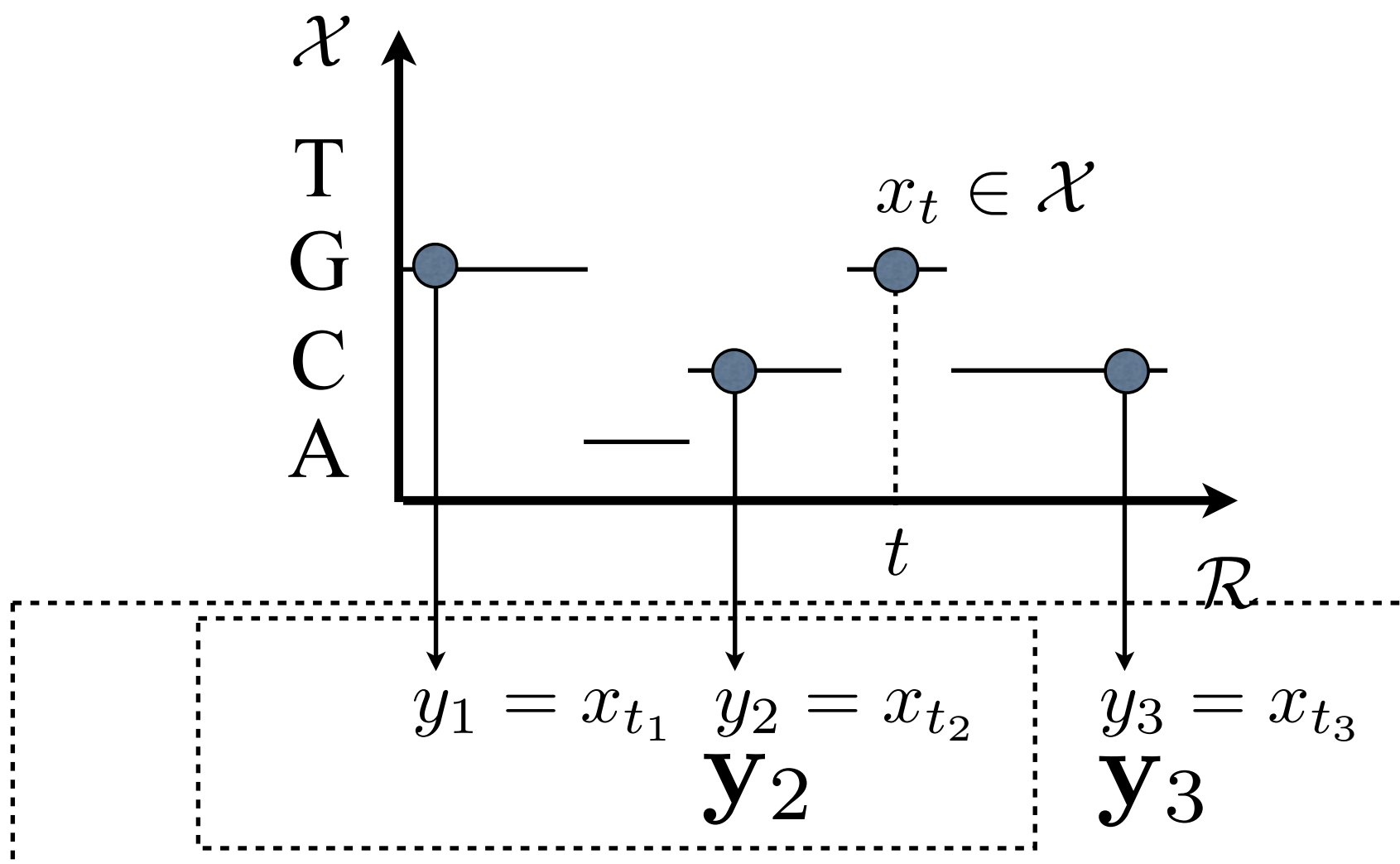
Subscript: process index

\mathbf{X}_t

Many points in the state space

\mathbf{y}_t

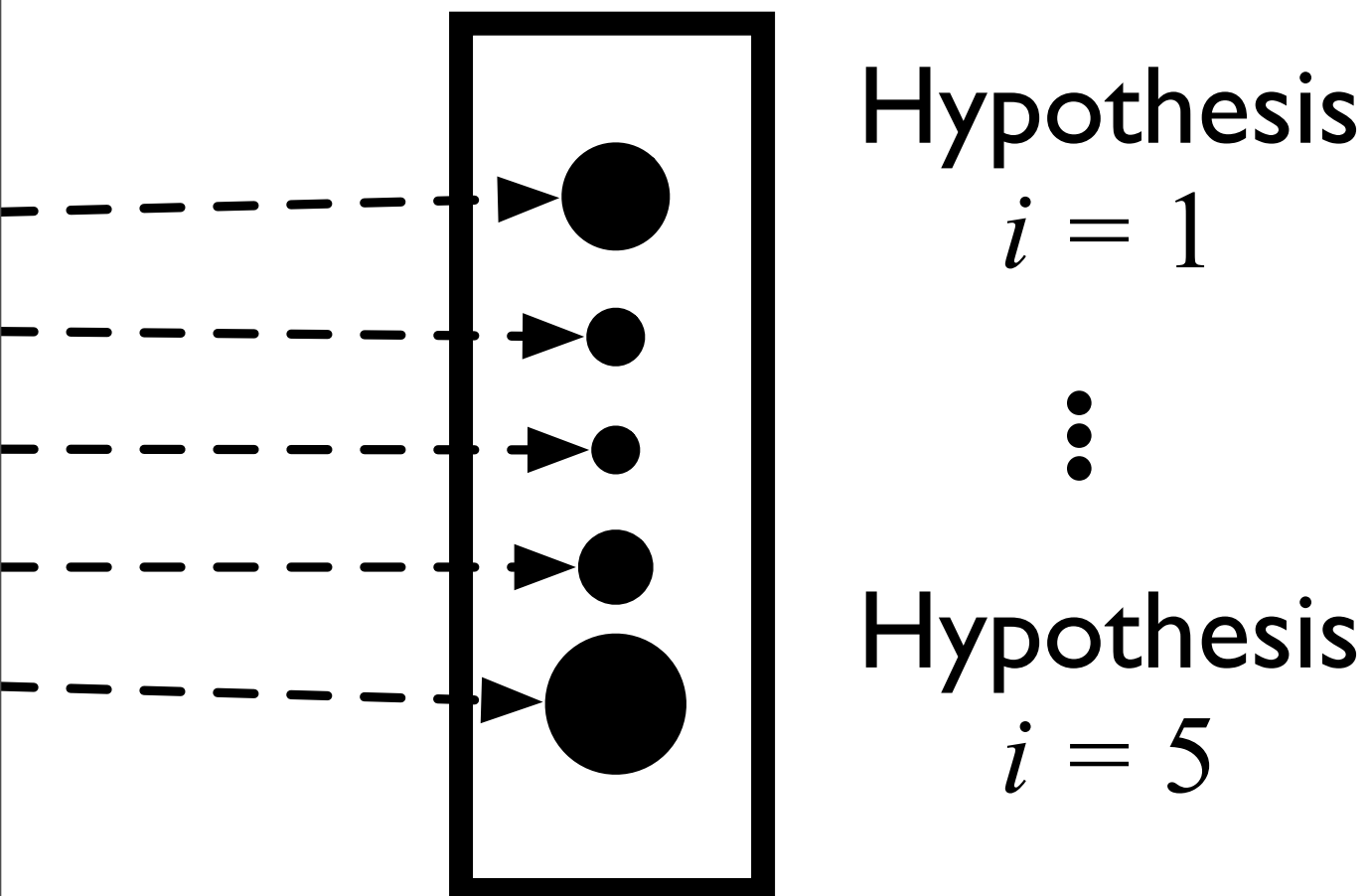
Many observations



Standard SMC

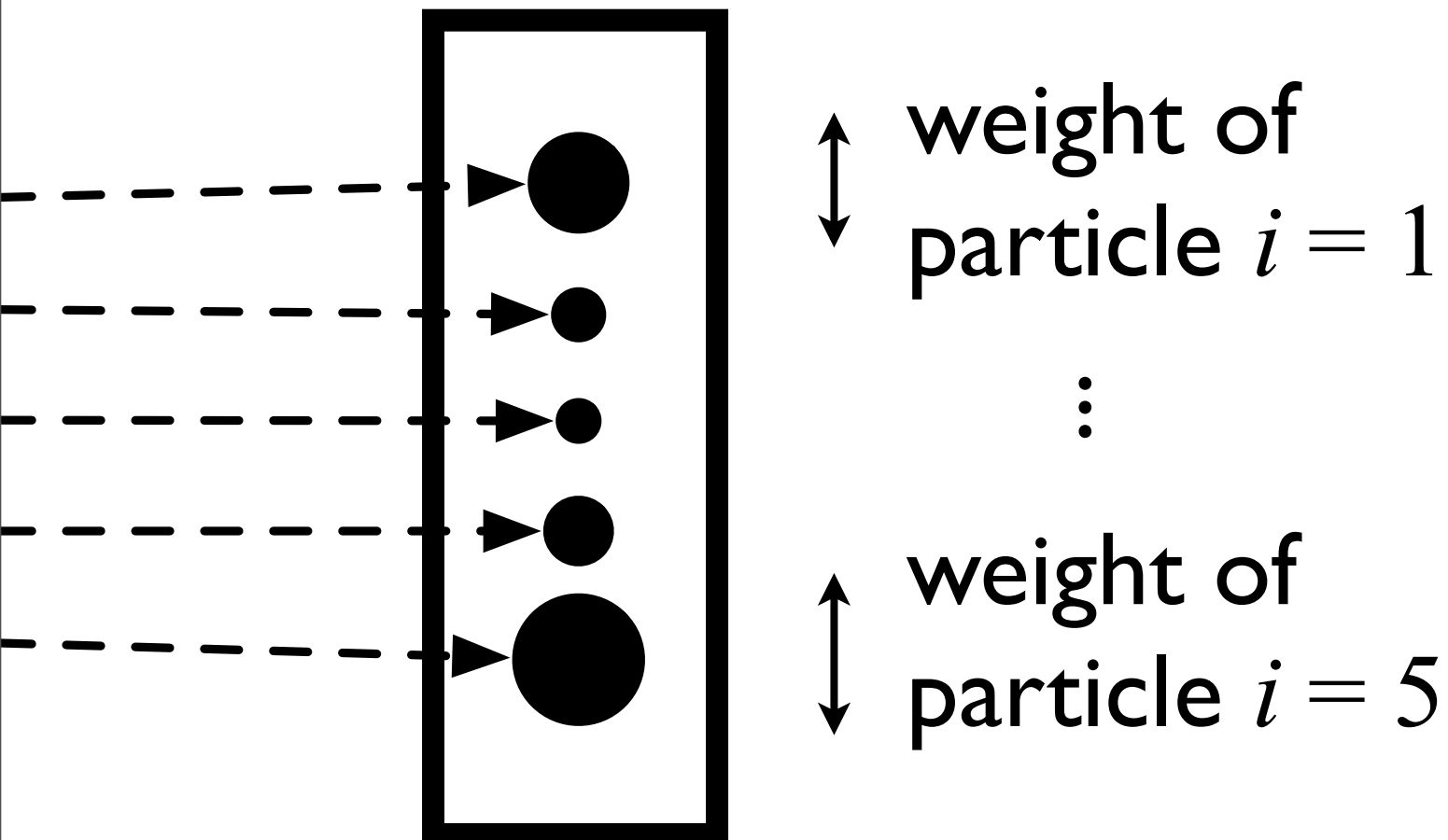
Output: competing 'hypotheses' \mathbf{X}_t^i

$t =$ last time observed



Standard SMC

Output: competing 'hypotheses' \mathbf{x}_t^i
weight for each of these w_t^i

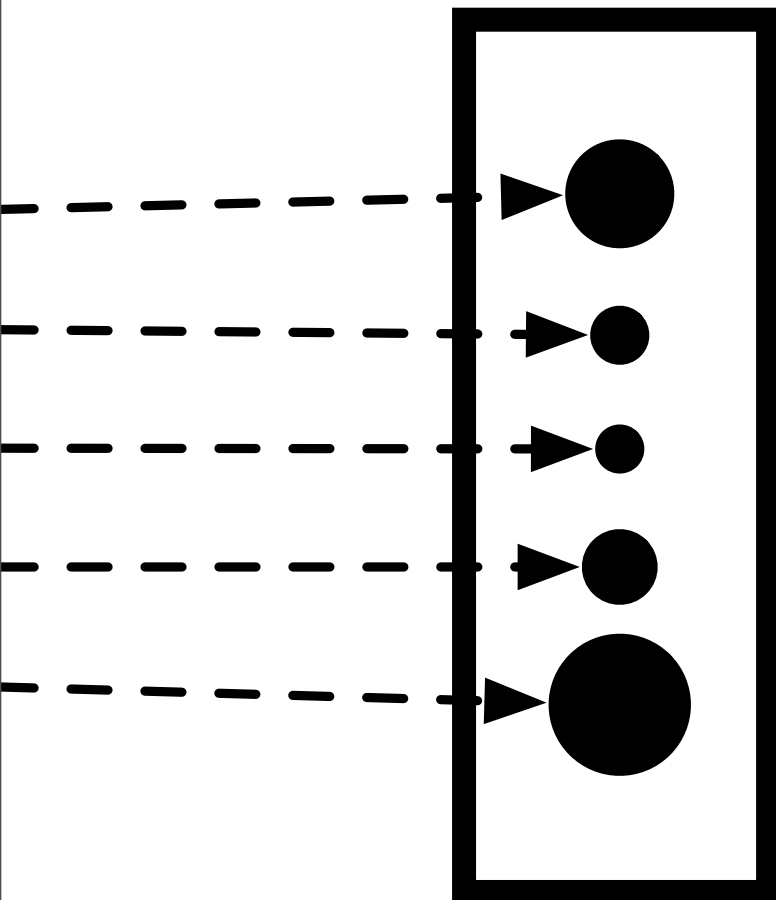


Standard SMC

Output: competing 'hypotheses' \mathbf{x}_t^i
weight for each of these w_t^i



Can view these as a (random) distribution

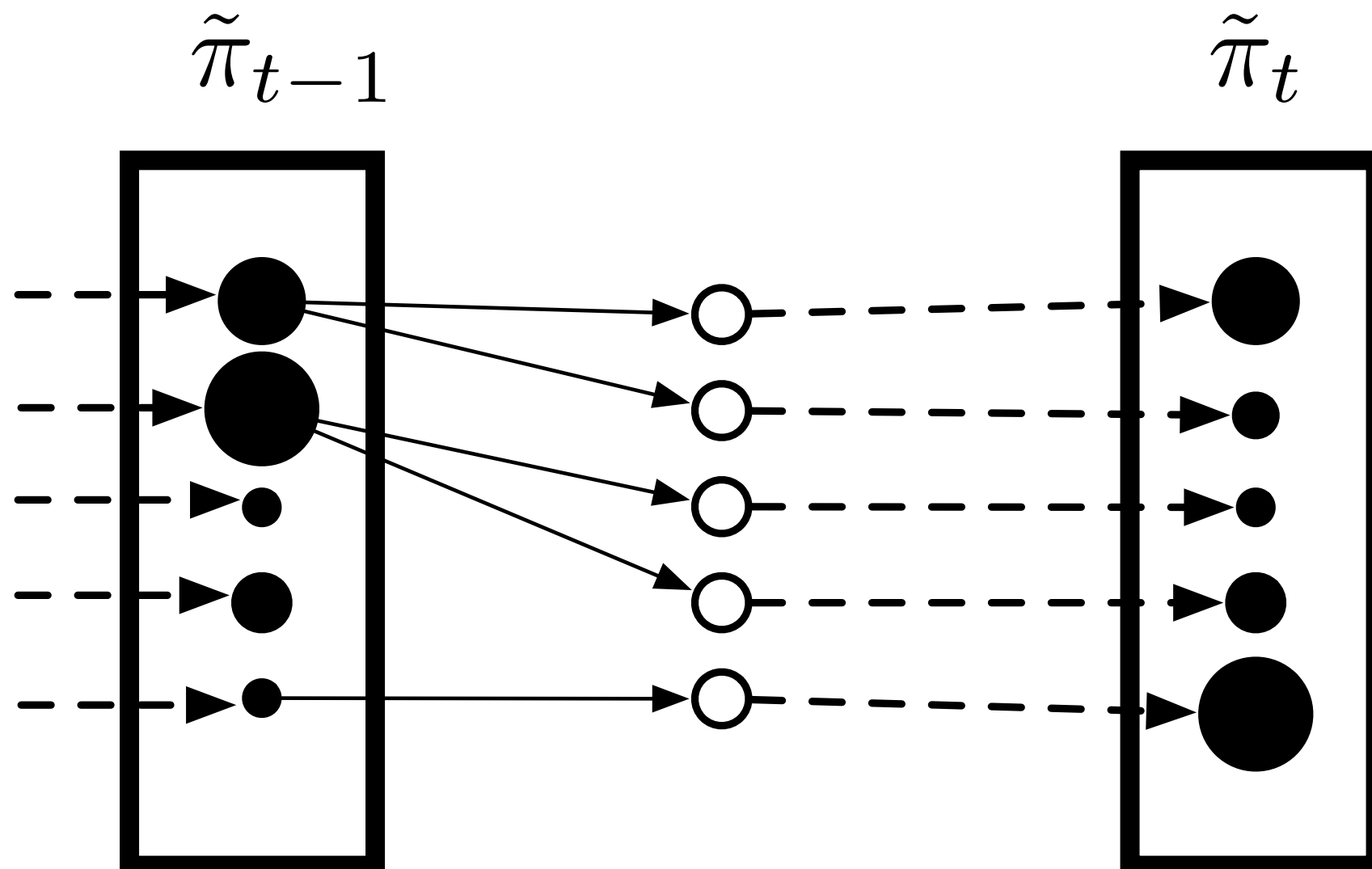


$$\tilde{w}_t^i = \frac{w_t^i}{\sum_j w_t^j}$$
$$\tilde{\pi}_t(\cdot) = \sum_i \tilde{w}_t^i \delta_{\mathbf{x}_t^i}(\cdot)$$

Standard SMC

inner working: I. Assume inductively that we have computed approximation for:

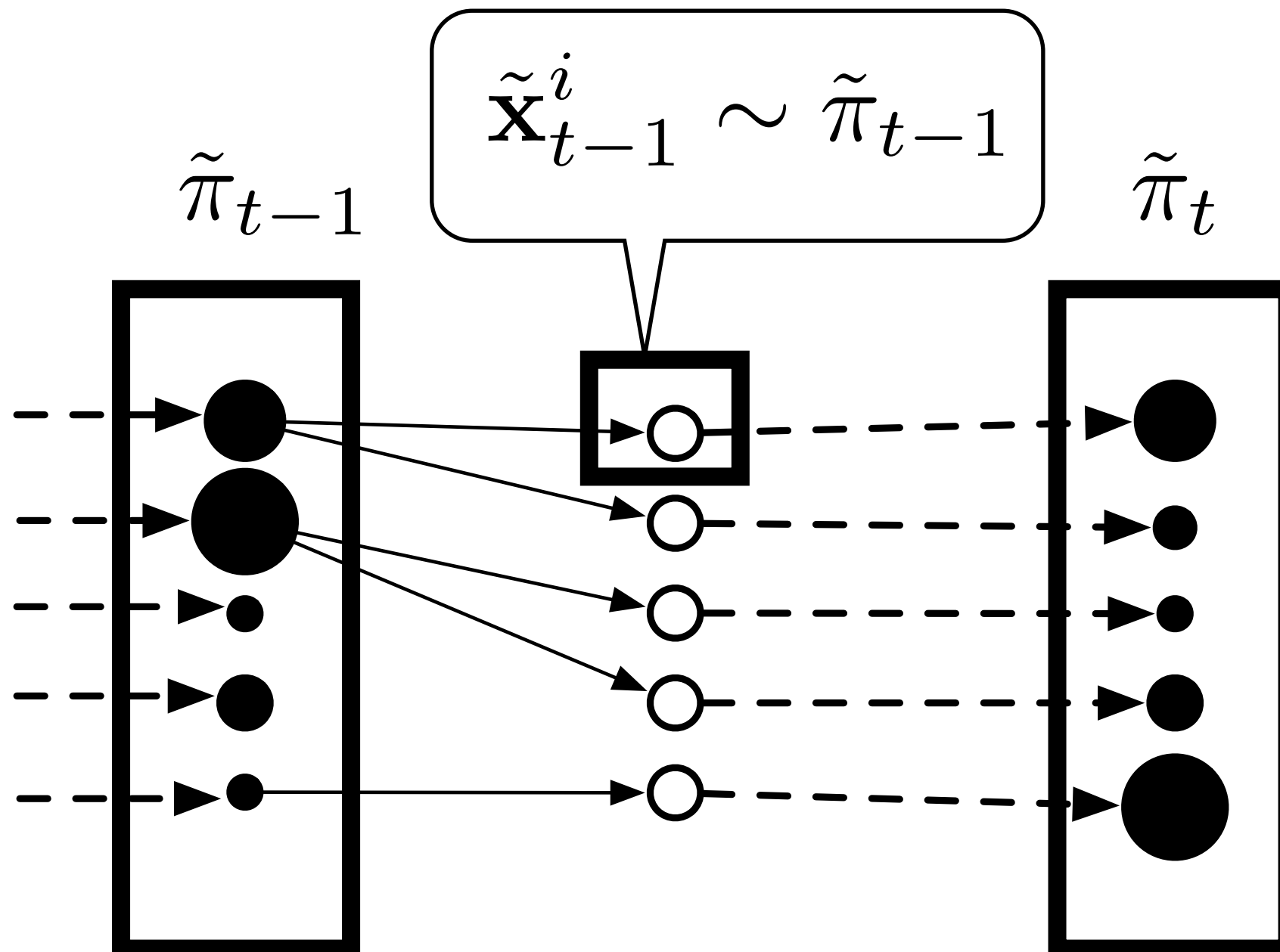
$$\pi_{t-1}(\mathbf{x}_{t-1}) = p(\mathbf{x}_{t-1} | \mathbf{y}_{t-1})$$



Standard SMC

inner working: 1. Assume inductively..

2. Sample from $\tilde{\pi}_{t-1}$



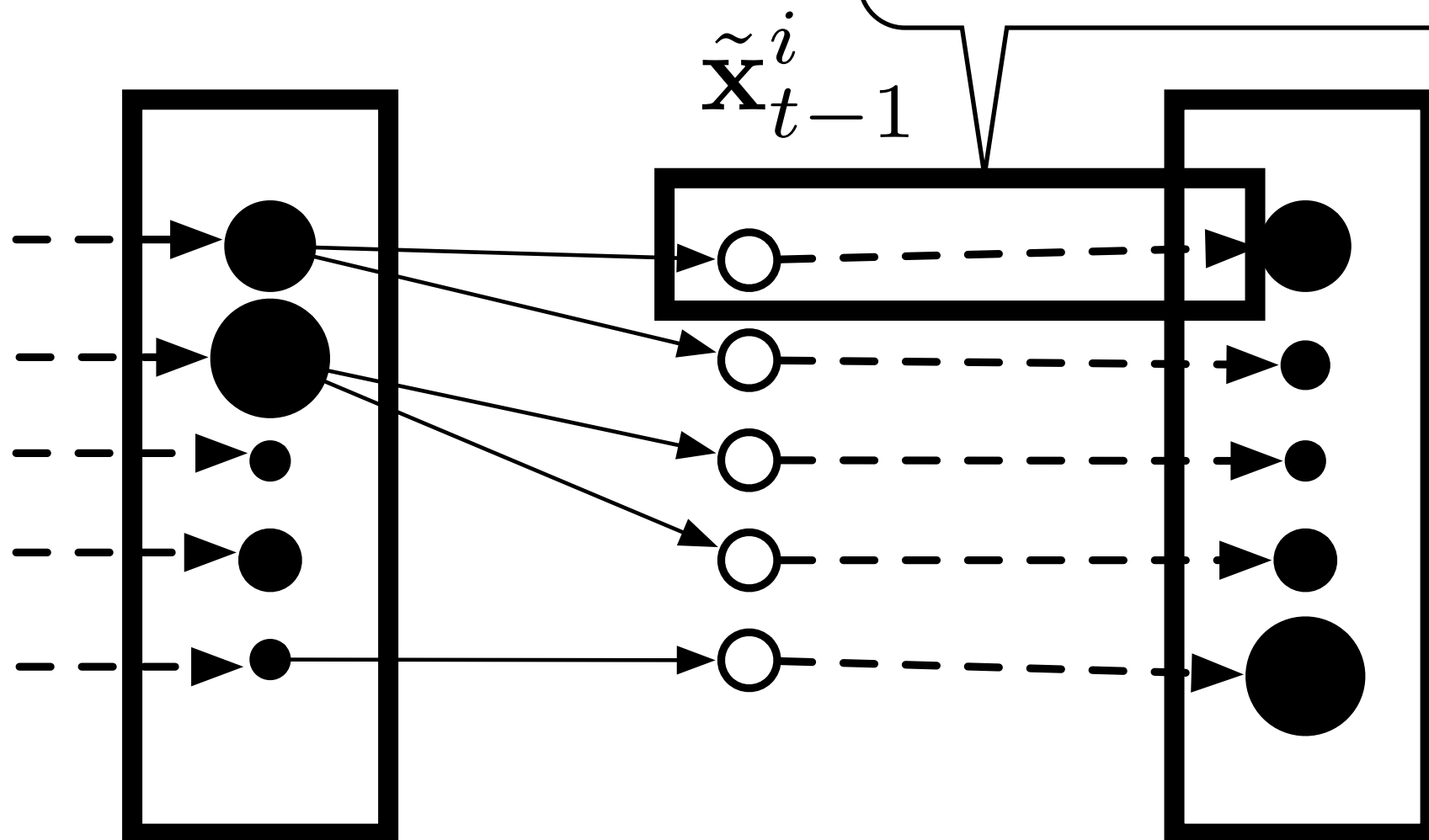
Standard SMC

inner working: 1. Assume inductively..

2. Sample from $\tilde{\pi}_{t-1}$

3. Propose (extend):

$$x_t | \tilde{\mathbf{X}}_{t-1} \sim q_t(\cdot | \tilde{\mathbf{X}}_{t-1})$$



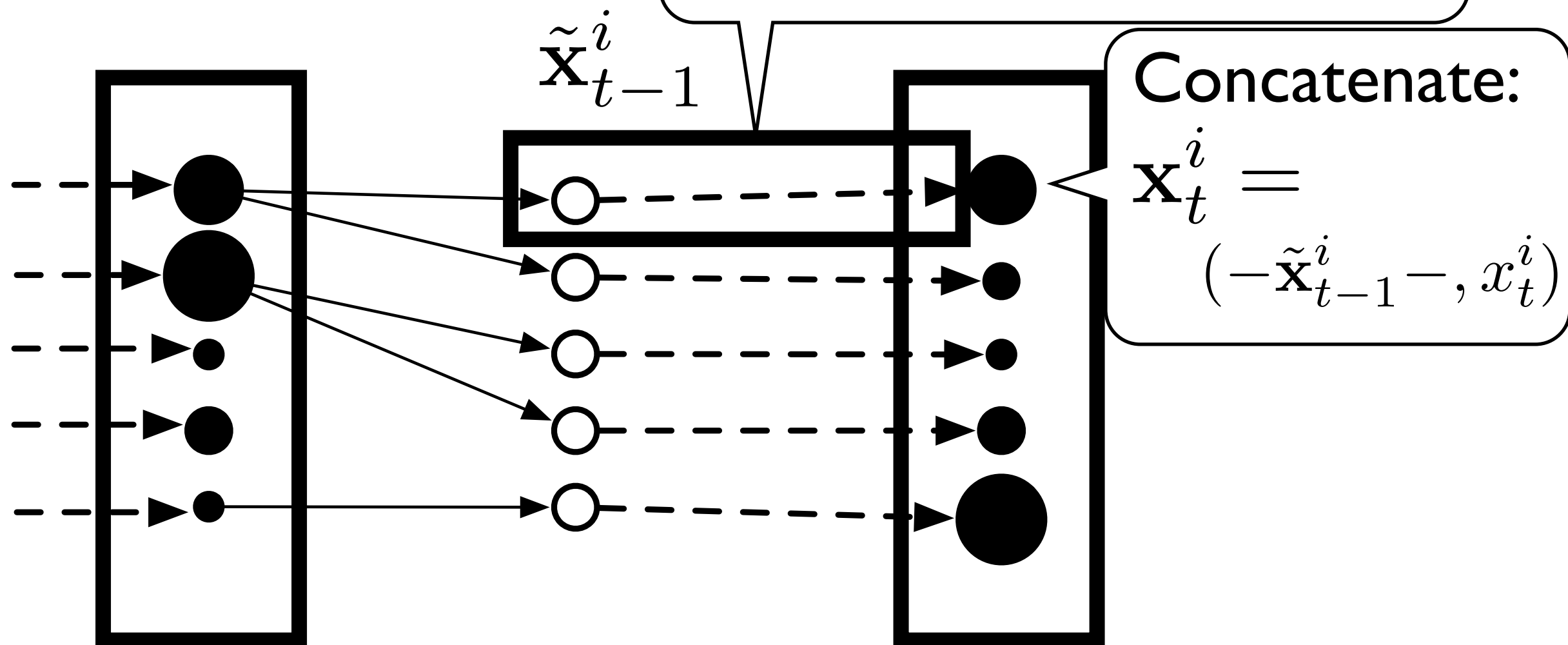
Standard SMC

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Standard SMC

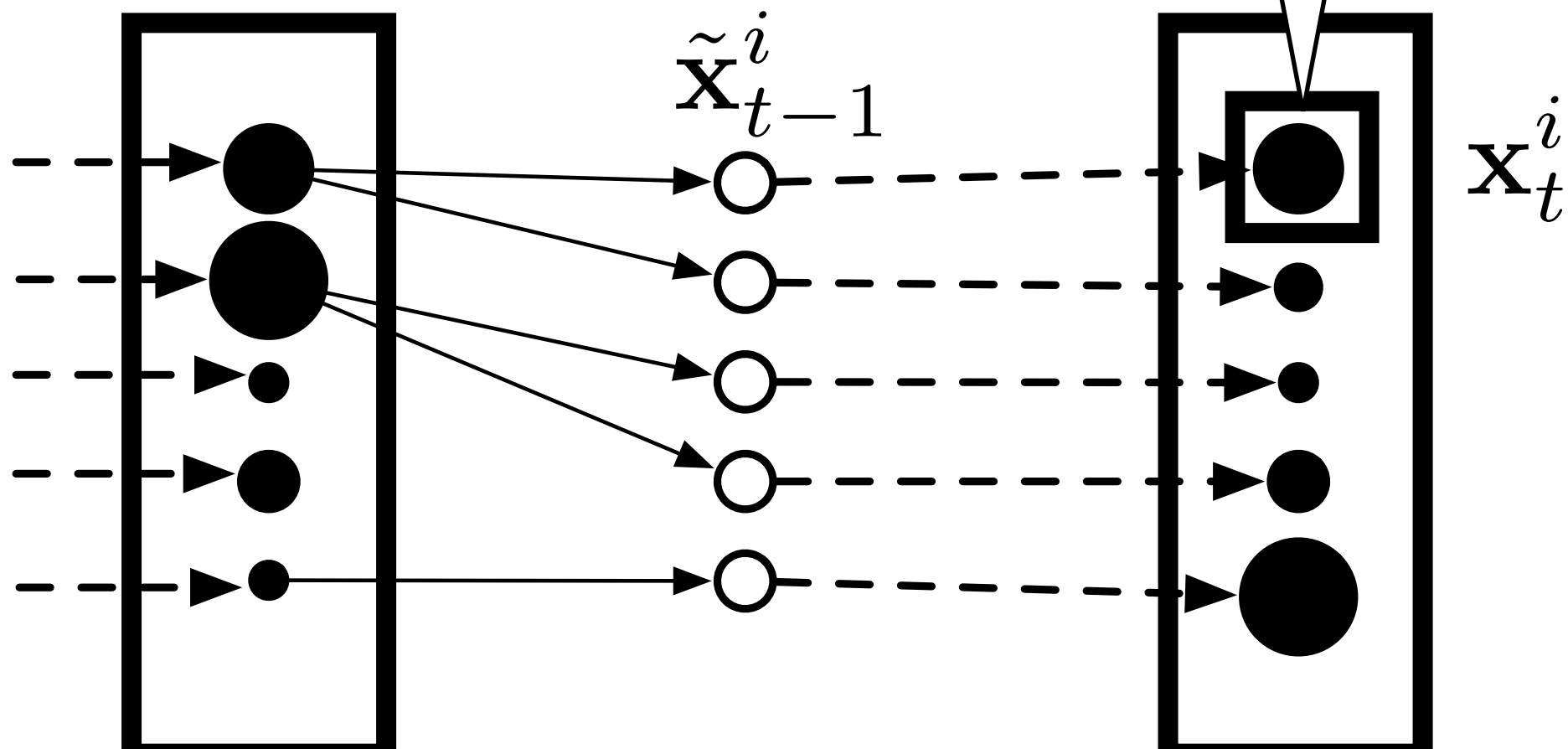
inner working: 1. Assume inductively..

2. Sample from $\tilde{\pi}_{t-1}$

3. Propose (extend)

4. Reweigh:

$$w_t^i = \frac{\pi_t(\mathbf{x}_t^i)}{\pi_{t-1}(\tilde{\mathbf{x}}_{t-1}^i) q_t(x_t^i | \tilde{\mathbf{x}}_{t-1}^i)} \cdot 1$$

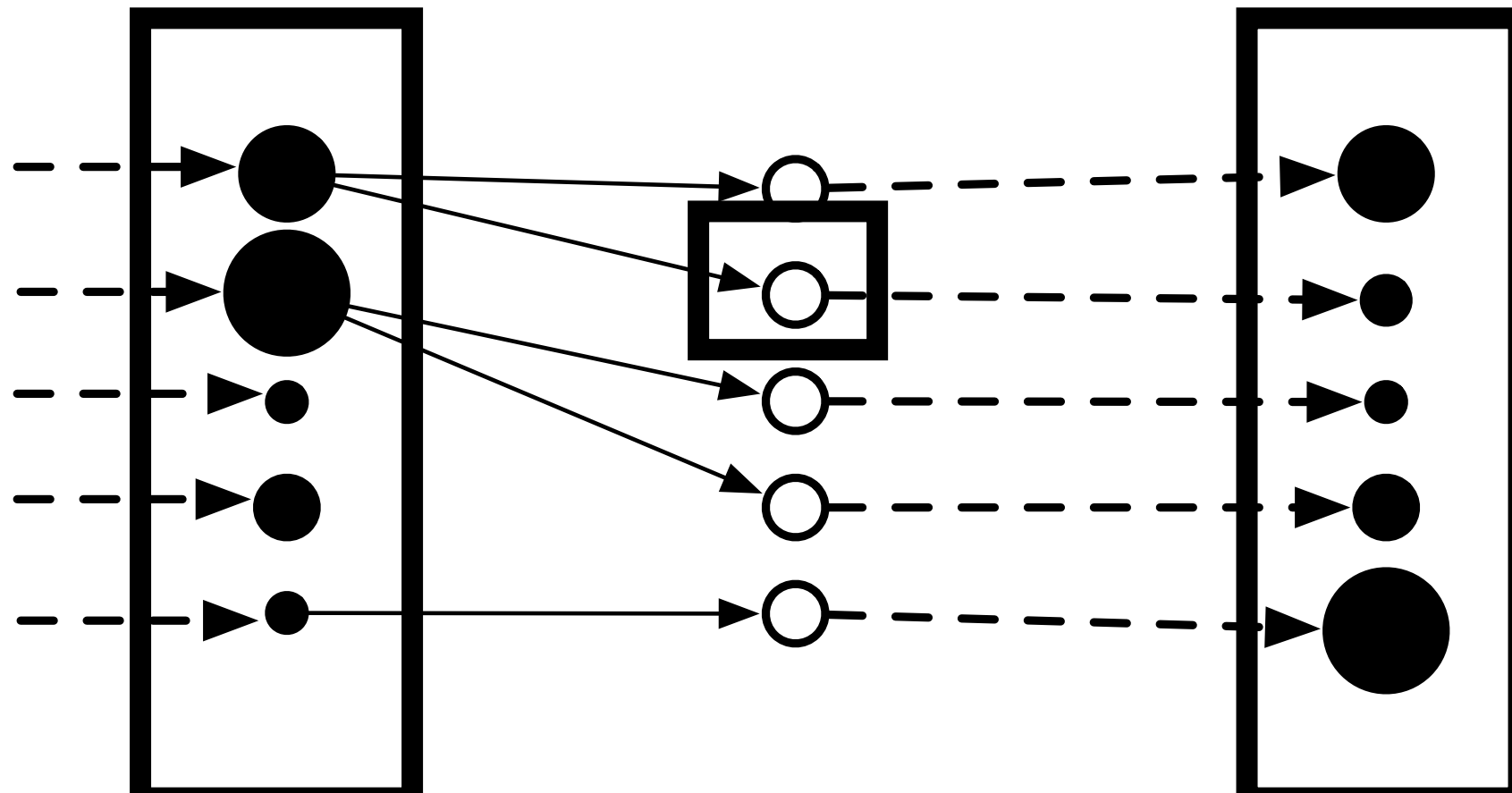


Standard SMC

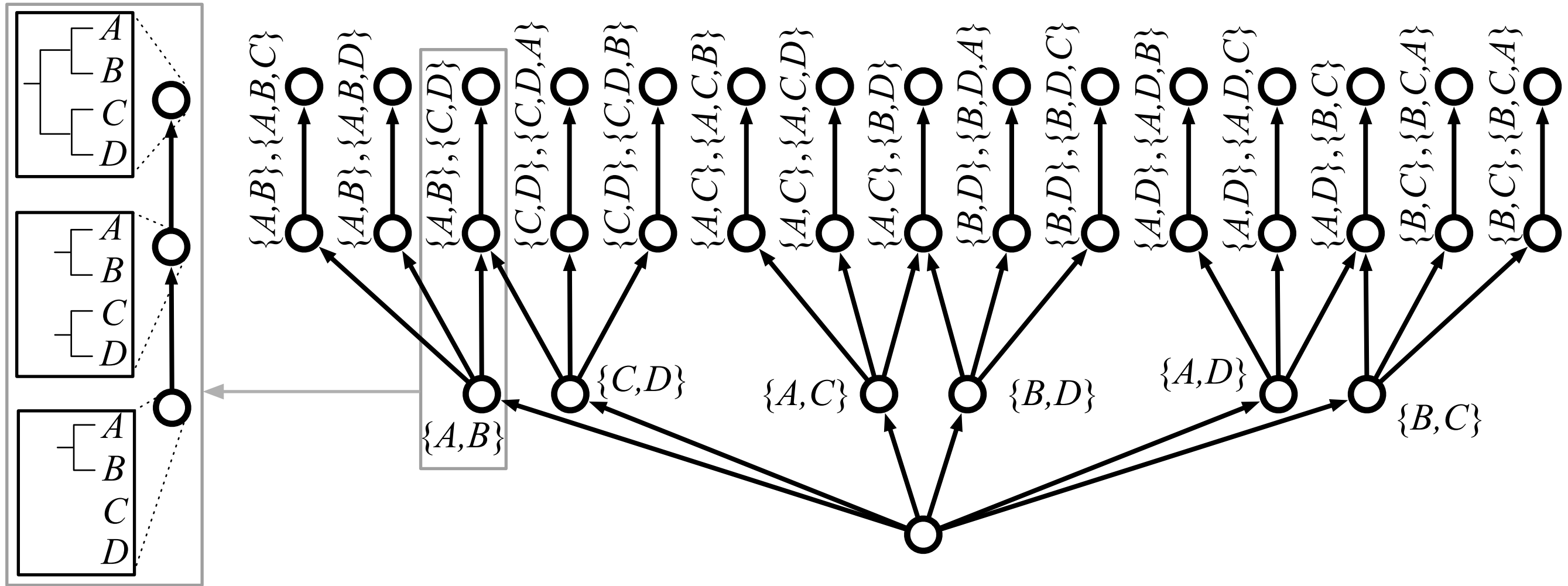
inner working: 1. Assume inductively..

Repeat for
each particle
(5 times)

2. Sample from $\tilde{\pi}_{t-1}$
3. Propose (extend)
4. Reweigh



Poset structure



Removing cycles with an auxiliary space

