


```
Call: glm(formula = cbind(deaths, litsize - deaths) ~ trtmnt,
          family = binomial)
```

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-2.1785	0.3046	-7.153	8.51e-13 ***
trtmntnone	3.3225	0.3308	10.043	< 2e-16 ***
trtmnt0/7	-1.1537	0.7814	-1.476	0.140
trtmntweekly	-0.8071	0.5503	-1.467	0.142

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 509.43 on 57 degrees of freedom
 Residual deviance: 173.45 on 54 degrees of freedom
 AIC: 252.92

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```
Call: glm(formula= cbind(deaths, litsize-deaths) ~ trtmnt,
          family = quasibinomial)
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-2.1785	0.5155	-4.226	9.23e-05 ***
trtmntnone	3.3225	0.5600	5.933	2.18e-07 ***
trtmnt0/7	-1.1537	1.3227	-0.872	0.387
trtmntweekly	-0.8071	0.9315	-0.867	0.390

(Dispersion parameter for quasibinomial family
 taken to be 2.864945)

Null deviance: 509.43 on 57 degrees of freedom
 Residual deviance: 173.45 on 54 degrees of freedom
 AIC: NA

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Comfortable doing inference without a real model?

Say Y is a random variable taking values in $\{0, \dots, n\}$ with mean np and variance $\phi np(1-p)$. Can show $\phi < n$.

Note that in the Rats data ex., $\hat{\phi} = 2.86$, while $n_i = 1, 2$ for some litters.

What about using a real model with $v(\mu) > \mu(1-\mu)$ for "binomial" data, or $v(\mu) > \mu$ for "Poisson" data.

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Negative-Binomial Distribution

This family of distributions can be parameterized as $E(Y) = \mu$, $Var(Y) = \mu + \mu^2/\theta$.

So have a GLM, but with an unknown parameter in the variance function (does complete fitting algorithm).

Connection to usual parameterization, $Y \sim$ number of failures in sequence of independent trials performed until α successes are seen, where p is success probability for each trial?

More relevant representation of NB distribution as a **mixture**.

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```

> ### simulate neg-binom data
> set.seed(13)
> n <- 100
> x1 <- rnorm(n); x2 <- .8*x1 + sqrt(1-.8^2)*rnorm(n)
> mu <- exp(1+.25*x1)
> mu2 <- mu*(rgamma(n,3)/3)
> y <- rpois(n,mu2)

> fit3 <- glm(y~cbind(x1,x2),family=poisson)
> fit4 <- glm(y~cbind(x1,x2),family=quasipoisson)
> library("MASS")
> fit5 <- glm.nb(y~cbind(x1,x2))

```

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```
Call: glm(formula = y ~ cbind(x1, x2), family = poisson)
```

Deviance Residuals:

	Min	1Q	Median	3Q	Max
	-3.0262	-1.3048	-0.4312	0.7770	4.4132

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	1.11110	0.05781	19.218	< 2e-16 ***
cbind(x1, x2)x1	0.29669	0.08992	3.300	0.000969 ***
cbind(x1, x2)x2	-0.07716	0.08815	-0.875	0.381410

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 240.42 on 99 degrees of freedom
Residual deviance: 224.11 on 97 degrees of freedom
AIC: 483.19

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```
Call: glm(formula = y ~ cbind(x1, x2),
          family = quasipoisson)
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	1.11110	0.08679	12.802	<2e-16 ***
cbind(x1, x2)x1	0.29669	0.13499	2.198	0.0303 *
cbind(x1, x2)x2	-0.07716	0.13234	-0.583	0.5612

(Dispersion parameter for quasipoisson family
taken to be 2.253698)

Null deviance: 240.42 on 99 degrees of freedom
Residual deviance: 224.11 on 97 degrees of freedom
AIC: NA

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```
Call: glm.nb(formula = y ~ cbind(x1, x2),
              link = log)
```

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	1.11061	0.08611	12.898	<2e-16 ***
cbind(x1, x2)x1	0.28608	0.13655	2.095	0.0362 *
cbind(x1, x2)x2	-0.05304	0.13282	-0.399	0.6897

(Dispersion parameter for Negative Binomial(2.4708)
family taken to be 1)

Null deviance: 117.46 on 99 degrees of freedom
Residual deviance: 110.11 on 97 degrees of freedom
AIC: 444.15

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Correlation of Coefficients:

(Intercept) cbind(x1, x2)x1

cbind(x1, x2)x1 -0.02

cbind(x1, x2)x2 -0.01 -0.74

Theta: 2.471

Std. Err.: 0.673

2 x log-likelihood: -436.149