A New Contamination Model

Ruben Zamar
Department of Statistics, UBC

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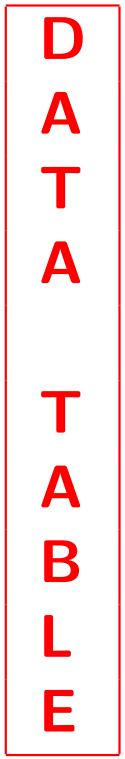
  - Percentage of unusual data points is relatively small
  - Hopefully way below 50%

The Shape of Data Tables

- Typical data table (before)



LARGE and Shallow Data Tables

- In some applications we deal with datasets like this

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- Asthenosphere Data

p	number of locations	about 5000
n	number of days	3650 days

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- Rows may be only partially spoiled
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- Need for more flexible robustness methods and models

An Example: Cell-wise Contamination Model

- From Alqallaf's PhD thesis and Alqallaf et al (2009)

$$\mathbf{X} = (I - B)\,\mathbf{Y} + B\mathbf{Z}$$

$$B = diag\,(B_1, B_2, ..., B_p)$$

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